# BT-5/D-21 <br> ADVANCED ALGORITHMS 

## Paper-PE-CS-T 307A

Time Allowed: 3 Hours]
[Maximum Marks : 75
Note : Attempt five questions in all, selecting at least one question from each Unit. All questions carry equal marks.

## UNIT-I

1. (a) Explain Big-oh, Big-omega and Big-theta notations of the complexity with suitable examples.
(b) What is Binary search tree? Write down the insertion algorithm of Binary search tree and insert the following elements: $35,29,17,44$, $55,67,3,2,114,55,15,28,88$, and 41 . Also, explain the problem of skewness in BST.

8
2. (a) Solve the following recurrence relation using Master theorem: 7 $T(n)=2 T(n / 4)+\sqrt{n}$
(b) Using recursive tree method solve the following:

8
$T(n)=T(n / 10)+T(9 n / 10)+n$

## UNIT-II

3. (a) What is Activity Selection problem? Solve following problem using greedy algorithm. Set of activity

$$
S=\left\{a_{1} a_{2}, a_{3}, a_{4}, a_{5}^{\prime}, a_{6}, a_{7}, a_{8}, a_{9}, a_{10}, a_{11}\right\}
$$

| $l$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s_{i}$ | 1 | 3 | 0 | 5 | 3 | 5 | 6 | 8 | 8 | 2 | 12 |
| $f_{i}$ | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |

(b) Explain the fundamental steps of finding longest common subsequence using dynamic programming. Find LCS between two strings $\mathrm{X}=\mathrm{BACDB}$ and $\mathrm{Y}=\mathrm{BDCB}$.
4. (a) Explain Strassen's algorithm to compute the matrix multiplication and analyze its complexity. Also multiply following matrix using Strassen's Algorithm.

$$
X=\left[\begin{array}{ll}
3 & 2 \\
4 & 8
\end{array}\right] \quad Y=\left[\begin{array}{ll}
1 & 5 \\
9 & 6
\end{array}\right]
$$

(b) Write Huffman code for following symbols

| Symbol | A | B | C | D | E | F |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 45 | 12 | 13 | 16 | 9 | 5 |

## UNIT-III

5. (a) Define spanning tree. Write the pseudo code of the Kruskal algorithm for finding minimum spanning tree. Also analyze its complexity.
(b) What is topological sort? Explain with an example.
6. (a) Explain Floyd-Warshall Algorithm to find all pair shortest path. Find all pair shortest path of following problem also analyze its complexity.

(b) Write shortest path Dijkstra Algorithm and explain its steps. UNIT-IV
7. (a) Write Naive string matching algorithm and explain its working with an example.
(b) Write Rabin-Karp string matching algorithm.
8. Explain different components of Knuth-Morris-Pratt algorithm and explain them by taking an example.
